

Mining Attributed Networks

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Tutorial Abstract. Research in modeling, analyzing and mining large-scale networks has attracted an increasing effort in the last few years. A major trend of work in network modeling and mining concerns analyzing homogeneous static networks (i.e., one snapshot of a network). However, in real world settings, networks are often dynamic, heterogeneous, and both nodes and links can be described by a set of attributes. To cope with that problem, two current main trends are explored in our tutorial: multiplex networks and attributed networks analysis approaches.

A multiplex network is often represented as a multi-layer network composed of a set of nodes related to each other with different types of relations. This representation is much richer than simple monoplex networks. However, this poses the challenge to provide adequate answers to all basic network analysis tasks that have been studied and provided in the recent few years. Almost all work in the field of multiplex and attributed network analysis are based on transforming the problem, in a way or another to the classical case of homogeneous network analysis. In this tutorial, we focus mainly on new approaches that extend existing approaches to new rich representations of multiplex and attributed networks, and provide an organized picture on analytical methods, also including exemplary applications.

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